Introduction	Model	Steady State	Welfare and Growth	Conclusion

# Endogenous Transport Investment, Geography, and Growth Take-offs

#### International Conference on Infrastructure Economics and Development

Stefan Zeugner

ECARES, Université Libre de Bruxelles (ULB)

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# Motivation: Geography Matters

#### Motivation

- Industrial revolution: why Britain?
- Why do some countries manage growth take-off and some don't?

 Stylized fact: inter alia, growth take-off is associated with rapid urbanization / agglomeration (cf. e.g. recent World Bank WDR 2009)

Economic Geography attributes both effects to falling transport costs
 but does not explain how these obtain.

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# Motivation: Transport matters

#### Economic Geography (NEG) Approach

 Economic Geography (Krugman, 1991, ...), theoretical: Spatial concentration depends on exogenous transport cost parameter:

- Two symmetric regions: Initially static gains from trade.
- If transport costs sink below a certain threshold: agglomeration
- ⇒ All modern firms cluster in one region (beneficial / 'take-off')

#### Critique

X In NEG, transport costs are causal to economic growth

- × Transport cost change is exogenous, arbitrary, and even for free!
- NEG does not explain why transport costs fall and if, why and when the threshold is reached

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#### Transport & Growth: Literature

- Empirical findings:
  - Transport infrastructure hardly causal to growth (e.g. Bose & Haque 2005)
  - Transport infrastructure is costly not easy to afford
  - Historically, a decrease in physical transport costs not tariffs is related to industrial revolution (O'Rourke 2000)
- Analytical models:
  - very few: Vishny & Shleifer (1989), Kelly (1997), NEG: Takahashi (2006)
  - coordinate investment into one technology with externalities (EoS): 'Big Push' – result is trivial

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**Objective:** Model that features

- **1** Static benefits from economic integration
- 2 Agglomeration-enhanced innovation
- 3 Endogenous transport that comes at a cost

 $1\ \&\ 2$ : Use Baldwin, Martin and Ottaviano (2001) NEG & growth model

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Note: Features borrowed from Baldwin et al. (2001) marked in grey

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#### Endogenize Transport



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Endogenize	e Transpo	ort		





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# Endogenize Transport: Fleet Investment

This paper concentrates on 'fleet investment': private, bottom-up transport capital, no (direct) externalities Each private firm builds improves its own 'fleet' of vehicles

- Why private bottom-up?
  - In 19th century Europe and poor countries, fixed transport infrastructure mostly built privately (Keller & Shiue 2008)
  - Most large infrastructure projects designed to meet private demand
- Why no externalities?
  - Majority of transport investment is in rolling stock (US) should apply even more to poor countries.
  - In 18th century Britain, transport improvements financed by private ventures and local merchants

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# Overall Transport Investment in the US



Investment in transport capital by household, private business, and government sector Data source: Bureau of Transport Statistics (2004)

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# Model Set-up: borrowed from Baldwin et al. (2001)

- Two regions, symmetrical endowments
- Two production factors: labor L,  $L^*$  and capital  $K + K^* = K^w$
- Three sectors:
  - Consumer good Agriculture (A): numéraire, perfect competition
  - Consumer good Manufacturing (M): monopolistic competition, standard mark-up pricing, profits accrue to capital owners
  - Innovation sector (I): AK productivity with localized spillovers  $A \equiv \frac{K}{K^{w}} + \lambda \frac{K^{*}}{K^{w}} = s + \lambda(1 - s) \qquad \lambda \in (0, 1)$
- Representative consumer: Cobb-Douglas between A and M, CES over manufacturing products (elasticity  $\sigma > 1$ )

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Geography:	Iceberg Co	osts		

- Trade agricultural goods at no cost (equalizes wages)
- Immobile L & K, K has to be employed where it is constructed
- Iceberg costs for manufacturing goods:
  - Need  $au \geq 1$  goods shipped for 1 unit to arrive in South  $( au^* v.v.)$
  - Thus export price  $p^* = \tau p$  ( $\tau$  times domestic price)
  - Define free-ness of trade  $\phi \equiv \tau^{1-\sigma} \in (0,1]$   $(\phi^* \text{ v.v.})$

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Fleet Invest	ment			

- Each firm i ships its goods by its own 'fleet'
- Fleet capital mapped to individual  $\phi_i \in (\phi, 1)$ :
  - $\blacksquare$  minimum value  $\phi$  and depreciation rate  $\delta_{\mathcal{T}}$
  - capital law of motion mapped to  $\dot{\phi}_i$
  - fleet investment rate  $Q_i$ , with quadratic adjustment costs

Firm's transport capital problem:

#### $\Rightarrow$ Dynamic system in $\phi_i$ and $\mathcal{Q}_i$ , unique steady state $(\widehat{\phi}, \widehat{\mathcal{Q}})$

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Fleet Investr	nent			

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  - **•** capital law of motion mapped to  $\dot{\phi}_i$
  - fleet investment rate  $Q_i$ , with quadratic adjustment costs
- Firm's transport capital problem:

$$\max_{Q_i} \int_0^\infty e^{-rt} (\overbrace{\pi_i(\phi_i)}^{\text{operating profits}} - \overbrace{a_T Q_i^2 w_L}^{\text{adjustment costs}}) dt$$
  
s.t.  $\frac{\dot{\phi}_i}{(1-\phi_i)} = (Q_i - \delta_T(\phi_i - \underline{\phi}))$ 

 $\Rightarrow\,$  Dynamic system in  $\phi_i$  and  $Q_i$ , unique steady state  $(\hat{\phi},\hat{Q})$ 

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Equilibriun	n and Ste	eady State		
Two kinds of	steady sta	te:		
Interior	Equilibrium	$\dot{K} = \frac{\dot{K}}{\kappa} = \frac{\dot{K}^*}{\kappa^*}$		

Two relations must hold in Steady State:

#### 'EE' Relation

 $\Rightarrow$  Northern income share  $s_E^{EE}(s) = \frac{E(s)}{E^w(s)}$  strictly increasing in s

• Core-Periphery (CP) Equilibrium:  $s \equiv \frac{K}{KW} = 1$  or s = 0

#### 'nn' Relation

 $\Rightarrow$  From equal return on capital (in interior equilibria):  $s_E^{nn}(s)$ 

⇒ Dynamics: CP and Symmetric  $(s_E^{nn} = s_E^{EE} = \frac{1}{2})$  are always solution, but may be *stable or unstable* 

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Equilibrium	and Steady	v State		
Two kinds of s	teady state:			

- Interior Equilibrium:  $\frac{\dot{K}}{K} = \frac{\dot{K}^*}{K^*}$
- Core-Periphery (CP) Equilibrium:  $s \equiv \frac{K}{K^w} = 1$  or s = 0

Two relations must hold in Steady State:

#### 'EE' Relation

$$\Rightarrow$$
 Northern income share  $s_E^{EE}(s) = \frac{E(s)}{E^w(s)}$  strictly increasing in  $s$ 

#### 'nn' Relation

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⇒ Dynamics: CP and Symmetric  $(s_E^{nn} = s_E^{EE} = \frac{1}{2})$  are always solution, but may be *stable or unstable* 

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#### Steady State: Phase Diagram



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# Isolation vs. Agglomeration

Initial Stage  $\phi=\phi$ 

Start from symmetric (stable) equilibrium  $\phi = \phi$ capital / real wage growth  $g_{iso} = bL^w \frac{1+\lambda}{2} - \Theta$ 

#### Intermediate Integration $\phi_{sym} > \phi$

If  $L^w$ ,  $\phi$  low: Firms build fleets  $\phi_{sym}$ , remain in symmetric steady state: Diverts resources from innovation to transport, lose on growth growth  $g_{sym} < g_{iso}$ 

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#### Rapid Agglomeration $\phi_{\it CP} > \phi_{\it sym}$

Only if  $L^w$ ,  $\underline{\phi}$  large enough: large  $\hat{\phi}_{CP}$  renders CP stable growth  $g_{CP} \ge g_{sym}$ 

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#### Simulation: From Isolation to Agglomeration



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Policy Implic	ations			

- This paper presents an endogenous growth model with growth take-offs – which may occur without government intervention
- Rather a role for government: complement private initiative, to push the economy to the CP steady state.
- Raising <u>\$\phi\$</u>: for instance, investing in *complementary public good* transport infrastructure ('ports'), removing obstacles, ...
- Decreasing fleet maintenance cost  $\delta_T$
- Reasons for lack of rolling infrastructue (e.g. Congo river, some rail lines)

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Introduction	Model	Steady State	Welfare and Growth	Conclusion
Conclusion				

- Endogenized transport infrastructure in Economic Geography via 'fleet investment': decentral, local, and endogenous
- $\Rightarrow\,$  resolves causality shortcomings in the literature
  - Result: Economic density L<sup>w</sup> vs. <u>\u03c6</u> determines *if*, *why*, *when* & *where* economies reach an 'agglomeration threshold' / 'take-off'
  - Note: Case with transport monopoly (same technology) yields broadly similar results

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References	Credit Constraints	Data	Model	Steady State	Simulation	Alternative Transport Sector
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- 6 Credit Constraints
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- 8 Model
- 9 Steady State
- **10** Simulation
- Alternative Transport Sector



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Firms may not be able to embark on their investment trajectory right away due to credit restrictions:

#### Export profitability constraint (EPC)

Operating profits from export  $\pi_i^*(\phi_i)$  larger than fleet maintenance cost

 $\pi_i^*(\phi_i) \geq a_T Q_i^2$ 

References Credit Constraints Data Model Steady State Simulation Alternative Transport Sector

# Fleet Investment with Export Profitability Constraint



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Firms may not be able to embark on their investment trajectory right away due to credit restrictions:

#### Export profitability constraint (EPC)

Operating profits from export  $\pi_i^*(\phi_i)$  larger than fleet maintenance cost

$$\pi_i^*(\phi_i) \ge a_T Q_i^2$$

- In case initial investment costs too expensive, firms invest little and move along the EPC until they hit the standard saddle path
- $\Rightarrow$  will severely delay time until steady state is reached
- ⇒ but has no effect on the position of steady state  $\hat{\phi}$ , CP or symmetric (since EPC is never binding in steady state)

References	Credit Constraints	Data	Model	Steady State	Simulation	Alternative Transport Sector

# Backup: Urbanization and Growth go Hand-in-Hand



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## Backup: Economic Density and Growth are Concurrent



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#### Backup: Take-off vs. Economic Density



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#### Backup: Infrastructure Stocks and GDP/cap.



# Backup: Fleet Dynamics

 $\dot{Q}_i$  from f.o.c.:

$$\dot{Q}_i = \left(
ho + \delta_{\mathcal{T}}(1-\phi)
ight) Q_i - rac{\partial \pi(\phi)}{\partial \phi} rac{(1-\phi)}{2 a_{\mathcal{T}} w_L}$$

Loci:

$$\begin{aligned} Q_i(\phi_i)|_{\dot{\phi}_i=0} &= \delta_T \left(\phi_i - \underline{\phi}\right) \\ Q_i(\phi_i)|_{\dot{Q}_i=0} &= \frac{\partial \pi(\phi)}{\partial \phi} \frac{(1-\phi)}{2a_T w_L \left(\rho + \delta_T (1-\phi)\right)} \end{aligned}$$

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# Backup: Transport Capital I

- Suppose transport capital  $K_i^T$  s.th.  $\phi_i(K_i^T) : [0, \infty) \to (0, 1]$ , monotone
- Firm's problem:

$$\max_{p_{i,t},p_{i,t}^{*},Q_{i,t}} \int_{0}^{\infty} e^{-rt} (x_{i}(p_{i,t})p_{i,t} + x_{i}^{*}(p_{i,t}^{*},\phi(K_{i,t}^{T}))p_{i,t}^{*} - F - - w_{L}a_{M} \left( x_{i}(p_{i,t}) + \tau x_{i}^{*}(p_{i,t}^{*},\phi(K_{i,t}^{T})) \right) - C(\overline{Q}_{i,t},K_{i,t}^{T})w_{L}) dt s.t. \quad \dot{K}_{i}^{T} = \overline{Q}_{i} - \overline{\delta}_{T}K_{i}^{T}$$

 Under no uncertainty, simultaneous optimization equivalent to sequential optimization:

$$\max_{Q_i} \int_0^\infty e^{-rt} \left( \pi_i(\phi_i(K_i^T)) - C(\overline{Q}_i, K_i^T) w_L \right) dt$$
  
s.t.  $\dot{K}_i^T = \overline{Q}_i - \overline{\delta}_T K_i^T$ 

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Specific parametrization:

$$\phi_i = \frac{K_i^T + \phi}{K^T + 1} \Leftrightarrow K_i^T = \frac{\phi - \phi}{1 - \phi} \qquad C(\overline{Q}_i, K_i^T) = a_T \left(\frac{\overline{Q}}{K + 1}\right)^2$$

• As  $\phi_i$  is bijective to  $K_i^T$ , express  $K_i^T$  in terms of  $\phi_i$ 

• Redefine 
$$Q_i \equiv \frac{\overline{Q_i}}{K_i+1}$$
,  $\delta_T \equiv \frac{\overline{\delta}_T}{(1-\underline{\phi})}$ 

 $\Rightarrow$  Reduced problem:

$$\max_{Q_i} \int_0^\infty e^{-rt} \left( \pi_i(\phi_i) - w_L a_T Q_i^2 \right) dt$$
  
s.t.  $\dot{\phi}_i = (1 - \phi_i) \left( Q_i - \delta_T(\phi_i - \underline{\phi}) \right)$ 



#### Fleet Investment: Additional Assumptions

#### Spillovers: capital stock *K* eases transport

- Basic Assumption: spillovers from capital stock extend to fleet investment
- Technical Assumption: for analytical tractability, specific transport capital productivity  $(s + \phi(1 s)) K^w$ , i.e. akin to capital spillovers

#### Transport: Constant Returns to Scale

The transport capital technology is CRS with respect to the number of shipped goods

References	Credit Constraints	Data	Model	Steady State	Simulation	Alternative Transport Sector
Backu	p: Market (	Cleari	ng			

- $\blacksquare$  Free trade in agriculture  $\Rightarrow$  agricultural price equals wage:  $w_L = w_L^* = 1$
- $\Rightarrow$  'mill price' of manufacturing good normalized to  $p_i = 1$ , Southern import price  $\tau_i \ge 1$
- $\Rightarrow$  Northern manufacturing firm operating profits:

$$\pi = \frac{\mu}{\sigma} \frac{E^{w}}{K^{w}} \left( \frac{s_{E}}{s + \phi^{*}(1 - s)} + \phi \frac{(1 - s_{E})}{\phi s + (1 - s)} \right)$$

 $\Rightarrow$  Northern consumption expenditure

$$E = \frac{L^w}{2} + (\pi - a_T Q^2) s K^w - L_I$$



# Backup: Steady State – Return on Capital

At any steady state: firm present value v equals capital cost a<sub>1</sub> for North and South:

$$v = \frac{\pi - a_T Q^2}{\rho + \delta + g} = \frac{1}{AK^w} = a_I \qquad v^* = a_I^*$$

 $\Rightarrow$  Pins down expenditure in both interior and CP steady state:

$$E(s) = \frac{L^{w}}{2} + \rho \frac{s}{A}$$
  $E^{*}(s) = \frac{L^{w}}{2} + \rho \frac{(1-s)}{A^{*}}$ 

 $\Rightarrow$  Returns  $\hat{\phi}$ ,  $\hat{Q}$  as a function of s



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 $\Rightarrow$  Returns  $\hat{\phi}$ ,  $\hat{Q}$  as a function of s

#### Backup: Steady State – Fleet

$$egin{aligned} \left(1-\hat{\phi}(s)
ight) &= -rac{rac{b}{2\delta_T^2} E^* + rac{
ho}{\delta_T} - (1-rac{
ho}{2})}{2} + \ &+ \sqrt{\left(rac{2\delta_T^2}{2\delta_T^2} E^* + rac{
ho}{\delta_T} - (1-rac{
ho}{2})}{2}
ight)^2 + rac{
ho}{\delta_T} (1-rac{
ho}{2})} \end{aligned}$$

$$\hat{Q}^{2} = (\hat{\phi} - \underline{\phi})\delta_{T} \left(\delta_{T}(1 - \underline{\phi}) + \rho\right) - \frac{b}{2} \underbrace{\left(\frac{L^{w}}{2} + \rho \frac{(1 - s)}{A^{*}}\right)}_{=E^{*}} (1 - \hat{\phi})$$

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#### Backup: Steady State – 'EE' relation

• From E(s):  $\Rightarrow$  market clearing ('EE') relation  $s_E^{EE}(s) = \frac{E}{E^w}$  as a strictly increasing function of s

$$s_E^{EE} = \frac{\frac{1}{2}L^w + \rho\frac{s}{A}}{L^w + \rho\left(\frac{s}{A} + \frac{(1-s)}{A^*}\right)}$$

References

Steady State

Simulation

Alternative Transport Sector

#### Backup: Steady State – 'nn' relation

 From v = a<sub>I</sub>, v\* = a<sub>I</sub>\* at all interior equilibria: innovation sector earnings equalization:

$$A(\pi - a_T Q^2) = A^*(\pi^* - a_T^* Q^{*2})$$

 $\Rightarrow$  Defines 'nn' relation  $s_E^{nn}(s)$ 

$$s_E^{nn}(s) = \frac{\frac{1}{bE^w} \left( A \Delta \hat{Q}^2 - A^* \Delta^* \hat{Q}^{*2} \right) + \Delta \left( (1 - \hat{\phi} \lambda) - (1 + \hat{\phi})(1 - \lambda)s \right)}{\left( 1 - \hat{\phi} \hat{\phi}^* \right) \left( A^*s + A(1 - s) \right)}$$

#### Dynamics

I if  $s_E^{nn}(s) < s_E^{EE}(s)$ , then  $\dot{s} > 0$  (due to  $rac{v}{a_i} > rac{v^*}{a^*_i}$ )

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Simulation

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#### Dynamics

If 
$$s_E^{nn}(s) < s_E^{EE}(s)$$
, then  $\dot{s} > 0$  (due to  $\frac{v}{a_I} > \frac{v^*}{a_I^*}$ )

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#### Backup: Threshold for Agglomeration

Parameter settings for which the the symmetric steady state is unstable (above the surface)



Parametrization for this figure:  $\delta = 0.05$ ,  $\rho = 0.02$ ,  $\lambda = 0.5$ ,  $b = \frac{\mu}{\sigma} = 0.2$ 



# Backup: Isolation Trap

Parameter settings for which the export profitability constraint  $\pi_i^* \ge a_T Q_i^2$  is binding (below the surface)



Parametrization for this figure:  $\delta$  = 0.05,  $\rho$  = 0.02,  $\lambda$  = 0.5,  $b = \frac{\mu}{\sigma} = 0.2$ 

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# Backup: Alternative Transport Sector

Credit Constraints

- Monopolist with toll and no CRS: revenue accruing to shipper per firm: (θ - 1)τx<sub>i</sub><sup>\*</sup>; τx<sub>i</sub><sup>\*</sup> is exported goods of firm i.
- Results: firm profits downweighted by  $\left(\frac{\sigma}{\sigma-1}\right)^{1-\sigma} \Rightarrow$ ,  $\hat{\phi}_{monop} < \hat{\phi}_{fleet}$ .

Steady State

Simulation

- Moreover in sym. and CP steady state:  $E_{monop} < E_{fleet}$ .
- Broadly, mechanics are quite similar.
- Did not manage to analytically solve for  $s_E^{nn}$  and  $s_E^{EE}$  i.e. steady state.
- seems that all growth rates are lower since bE<sup>w</sup> term is downweighted.
- Downsides with my formulation:
  - Also at  $\phi$  there is toll
  - monopolist does not take effect on price level into account (i.e. one monopolist per firm)

Alternative Transport Sector